

## QUANTUM THEORY : REVISION OF SEC.3

1. The TISE, with appropriate assumptions, takes the form :  

$$-\left(\frac{S'}{\hbar}\right)^2 + \frac{iS''}{\hbar} + \frac{P^2(x)}{\hbar^2} = 0$$
Derive this and explain the symbols.
2. By expanding  $S$  in a power series, derive the form of the WKB wavefunction in a classically allowed region (eq 3.14 in the notes).
3. Explain all the assumptions that went into the WKB (ie say something appropriate about  $\lambda'$  and something about  $\hbar$ ).
4. Justify in physical terms the form of the prefactor in the WKB wavefunction  $1/\sqrt{p}$ . Explain why it means you need connection formulae.
5. By linearising the TISE around a turning point, obtain the differential eq. solved by Airy functions. ie  $\psi'' - z\psi = 0$  where  $z = (2mg/\hbar^2)^{1/3} (x - a)$ . What useful properties do the Airy functions  $Ai$  and  $Bi$  have, far from the turning points?
6. Explain why you need arrows in the connection formulae. (see handout)
7. Given eq 3.26, show that a potential well, with no rigid walls has a  $(n + \frac{1}{2})\pi$  quantization condition. Compare with Bohr-sommerfeld quantization condition.
8. Show that a potential well with one rigid wall has a  $(n + \frac{3}{4})\pi$  quantization condition.
9. Show that a potential well with two rigid walls has a  $(n + 1)\pi$  quantization condition.
10. Derive the WKB formula for tunneling  $T = e^{-2\Lambda}$ ... long derivation!